

2018-2019 Curriculum Guide

November 12- November 30

Eureka

Module 2: Two Dimensional & Three Dimensional Shapes



ORANGE PUBLIC SCHOOLS

OFFICE OF CURRICULUM AND INSTRUCTION

OFFICE OF MATHEMATICS

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Module 2 Performance Overview

- In Topic A, students find and describe flat shapes in their environment using informal language, without naming them at first. Students use the informal language of their everyday world to name and describe flat shapes without yet expressing mathematical concepts or using the vocabulary of geometry. They begin to describe shapes using correct terminology first using attributes of shapes such as triangles and rectangles using examples and non-examples.
- The lessons of Topic B replicate those of Topic A but with solid shapes. In addition, students recognize the presence of the flats within the solids.
- The module closes in Topic C with discrimination between flats and solids. A culminating task involves students in creating displays of a given flat shape with counter-examples and showing related solid shapes.
- Using relative position of objects (below, top of, behind) should be interwoven throughout the day in addition to every lesson in this module
- Daily number fluency practice in this new module is critical. There are two main goals of consistent fluency practice:
 - 1. To solidify the numbers of Module 1 and 2
 - 2. To anticipate the numbers of Modules 3, 4, and 5.
- Therefore, students continue to work extensively with numbers to 10 and fluency with addition and subtraction to 5.



Module 2: Two-Dimensional and Three-Dimensional Shapes November 12- November 30th

12 Days

Topic	Lesson	Lesson Objective:
Topic A:	Lesson 1	Find and describe flat triangles, squares, rectangles, hexagons, and circles using informal language without naming.
Dimensional Flat Shapes	Lesson 2	Explain decisions about classifications of triangles into categories using variants and non-examples. Identify shapes as triangles
	Lesson 3	Explain decisions about classifications of rectangles into categories using variants and non-examples. Identify shapes as rectangles
	Lesson 4	Explain decisions about classifications of hexagons and circles, and identify them by name. Make observations using variants and non-examples
	Lesson 5	Describe and communicate positions of all flat shapes using the words above, below, beside, in front of, next to, and behind
Topic B:	Lesson 6	Find and describe solid shapes using informal language without naming
Three Dimensional Solid Shapes	Lesson 7	Explain decisions about classification of solid shapes into categories. Name the solid shapes
Topic C:	Lesson 9	Identify and sort shapes as two-dimensional or three dimensional, and recognize two-dimensional and three dimensional shapes in different orientations and sizes
Dimensional and Three Dimensional Shapes	Lesson 10	Culminating task—collaborative groups create displays of different flat shapes with examples, non-examples, and a corresponding solid shape

End-of- Module Assessment (Interview Style: 3 days)
November 28-30th, 2018

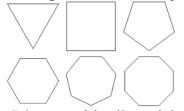
NJSLS Standards:

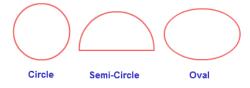
	Module 2: Two and Three Dimensional Shapes
K.G.1	Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinder and spheres)
 Describe the front of, below Example: to tions such a students by can) and to It is importate Example: A slide; triange is to clarify, 	bjects in the environment using names of shapes e relative positions of these objects using terms such as above, below, beside, in hind, and next to eacher can take students on a shape hunt in the class or outside and ask questas "What shape is the ball?" "Where is the ball?" to incorporate positional words wild on their knowledge of familiar objects from everyday life (ball, square box, make connections with mathematical vocabulary (sphere, cube, cylinder) and to be thoughtful in the selection of "real world" examples of shapes. It typical pizza slice is not a good example of a triangle because it has a curved gle have three straight sides. A way to help them address this misunderstanding the straight sides. What could we change to make the pizza slice a triangle?" we three straight sides)
K.G.A.2	Correctly names shapes regardless of their orientations or overall size
 Provide actidefine a sha Help childre Example: A 	dents to many shapes in different orientations and sizes ivities to talk about what a shape looks like and identify specific attributes that ape. en learn to describe and define shapes in terms of attributes (properties) Ask: what 'makes' this shape a triangle?" and guild students through attention to tures (ex. Three straight sides that touch)
K.G.A.3	Identify shapes as two dimensional (lying in a plan, "flat") or three dimensional ("solid")
	 This standard asks students to identify flat objects (2 dimensional) and solid objects (3 dimensional). This standard can be done by having students sort flat and solid objects, or by having students describe the appearance or thickness of shapes Example: arrange three objects for students to view such as a box, cone and a ball. Describe one of the objects, for instance, "all of its surfaces are flat". Have students tell which figure was described Students will describe cubes, cones, spheres, and cylinders as "solid" shapes because it can be measured in three different ways(length, width, and height) and hexagons, squares, rectangles, circles and triangles as "flat" shapes because it can be measured in only two ways (length and width)

	Teachers should be thoughtful about the language they use to describe shapes. Example: showing a picture of a cube and referencing it as a square. A cube is not an example of a square. The flat face of a cube is a square.
K.G.B.4	Analyze and compare two and three dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g. Number of sides and vertices/corners) and other attributes (e.g. having sides of equal length)



- Students explore the differences between two-dimensional and three-dimensional shapes
- Students look within those categories to compare and contrast shapes **Example**: students may set of two-dimensional shapes into two groups

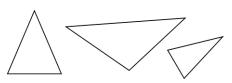


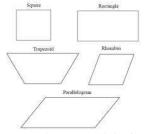


"shapes with all straight sides"

"shapes with curves"

Or students might sort a set of two-dimensional shapes based on the number of straight sides they have:





"shapes with three straight sides"

"shapes with four straight sides"

Students might also count the number of shapes in each group connecting to standard K.MD.3

- Understanding it is important that teachers make careful choices about shapes and shape-discussions in their classrooms.
 - **Example:** the attribute of a rectangle do not include "having two long sides and two short sides". A rectangle has four straight sides and four "square corners" (or right angles)
- Note that the orientation of a figure does not change the figure itself. <u>A diamond is not a geometric term and should not be used to describe shapes.</u>
- Provide tactile, hands-on experiences with constructing shapes while their fine motor skills

- are developing
- With repeated experiences drawing and building shapes, students become more precise and attend to attributes such as the shape's identity, types of sides (straight) (length)
- K.G.6 builds off of K.G.2- shapes can be turned (flipped/reflection, turns/rotations, slides/translations) and joined with other shapes to make new shapes
- The concept of composing and decomposing shapes is very important to students' future work with rectangular arrays and area models in later grades

K.MD.3

Classify objects into given categories; count the numbers of objects in each category and sort the categories by count.

- Students identify similarities and differences between objects (e.g., size, color, shape) and use the identified attributes to sort a collection of objects. Once the objects are sorted, the student counts the amount in each set. Once each set is counted, then the student is asked to sort (or group) each of the sets by the amount in each set. Thus, like amounts are grouped together, but not necessarily ordered.
- When exploring a collection of buttons:
 - * First, the student separates the buttons into different piles based on color (all the blue buttons are in one pile, all the orange buttons are in a different pile, etc.).
 - *Then the student counts the number of buttons in each pile: blue (5), green (4), orange (3), and purple (4).
 - *Finally, the student organizes the groups by the quantity. "I put the purple buttons next to the green buttons because purple also had (4). Blue has 5 and orange has 3. There aren't any other colors that have 5 or 3. So they are sitting by themselves."
- Ensure students have opportunities to explain how the objects are sorted into groups and how they categorized or labeled each set.
- This objective helps to build a foundation for data collection in future grades as they create and analyze various graphical representations.

M: Major Content

S: Supporting Content

A: Additional Content

Module 2 Assessmen	it / Authentic Assess Framework	sment Recom	mended	
Assessment	ccss	Estimated Time	Format	
Diagnostic Assessment (IREADY)		1-2 blocks	Individual	
<u>Eureka Math</u> <u>Module 2: Two & Three Dimensional Shapes</u>				
Culminating Task KMD3 K.G.1-4 30 mins Individual				
Optional End of Module Assessment (Interview Style)	KMD3 K.G.1-4	1 Block	Individual or Small Group with Teacher	

Kindergarten Ideal Math Block

Fluency: Whole Group Sprints, Counting, Whiteboard Exchange

Eureka Lesson Structure:

Fluency:

- Sprints
- Counting: Can start at numbers other than 0 or 1 and might include supportive concrete material or visual models
- Whiteboard Exchange

Application Problem:

- Engage students in using the RDW Process
- Sequence problems from simple to complex and adjust based on students' responses
- Facilitate share and critique of various explanations, representations, and/or examples.

Concept Development: (largest chunk of time)

Instruction:

- Maintain overall alignment with the objectives and suggested pacing and structure.
- Use of tools, precise mathematical language, and/or models
- Balance teacher talk with opportunities for peer share and/or collaboration
- Generate next steps by watching and listening for understanding

Problem Set: (Individual, partner, or group)

- Allow for independent practice and productive struggle
- Assign problems strategically to differentiate practice as needed
- Create and assign remedial sequences as needed

Student Debrief:

- Elicit students thinking, prompt reflection, and promote metacognition through student centered discussion
- Culminate with students' verbal articulation of their learning for the day
- Close with completion of the daily Exit Ticket (opportunity for informal assessment that guides effective preparation of subsequent lessons) as needed.

Number Talks

What does Number Talks look like?

- Students are near each other so they can communicate with each other (central meeting place)
- Students are mentally solving problems
- Students are given thinking time
- Thumbs up show when they are ready
- Teacher is recording students' thinking

Communication

- Having to talk out loud about a problem helps students clarify their own thinking
- Allow students to listen to other's strategies and value other's thinking
- Gives the teacher the opportunity to hear student's thinking

Mental Math

- When you are solving a problem mentally you must rely on what you know and understand about the numbers instead of memorized procedures
- You must be efficient when computing mentally because you can hold a lot of quantities in your head

Thumbs Up

- This is just a signal to let you know that you have given your students enough time to think about the problem
- If will give you a picture of who is able to compute mentally and who is struggling
- It isn't as distracting as a waving hand

Teacher as Recorder

- Allows you to record students' thinking in the correct notation
- Provides a visual to look at and refer back to
- Allows you to keep a record of the problems posed and which students offered specific strategies

Purposeful Problems

- Start with small numbers so the students can learn to focus on the strategies instead of getting lost in the numbers
- Use a number string (a string of problems that are related to and scaffold each other)

Starting Number Talks in your Classroom

- Start with specific problems in mind
- Be prepared to offer a strategy from a previous student
- It is ok to put a student's strategy on the backburner
- Limit your number talks to about 15 minutes
- Ask a question, don't tell!

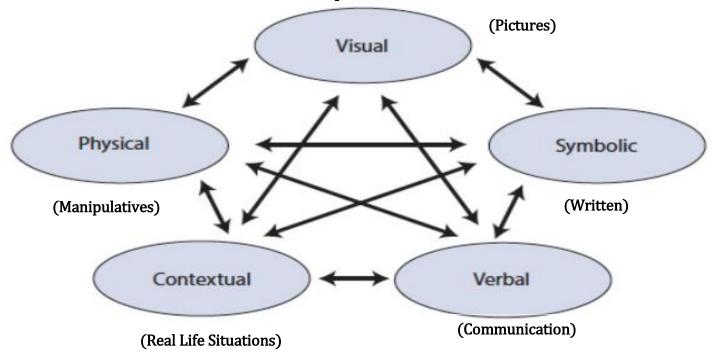
The teacher asks questions:

- Who would like to share their thinking?
- Who did it another way?
- How many people solved it the same way as Billy?
- Does anyone have any questions for Billy?
- Billy, can you tell us where you got that 5?
- How did you figure that out?
- What was the first thing your eyes saw, or your brain did?
- What are Number Talks and Why are they used?

Student Name:	Task:	School:	Teacher:	Date:
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		STUDENT FRI	RIENDLY RUBRIC		
"I CAN"	a start 1	getting there 2	that's it 3	WOW! 4	SCORE
Understand	I need help.	I need some help.	I do not need help.	I can help a class- mate.	
Solve	I am unable to use a strategy.	I can start to use a strategy.	I can solve it more than one way.	I can use more than one strategy and talk about how they get to the same answer.	
Say or Write	I am unable to say or write.	I can write or say some of what I did.	I can write and talk about what I did. I can write or talk about why I did it.	I can write and say what I did and why I did it.	
Draw or Show	I am not able to draw or show my thinking.	I can draw, but not show my thinking; or I can show but not draw my thinking;	I can draw and show my thinking	I can draw, show and talk about my thinking.	

Use and Connection of Mathematical Representations



The Lesh Translation Model

Each oval in the model corresponds to one way to represent a mathematical idea.

Visual: When children draw pictures, the teacher can learn more about what they understand about a particular mathematical idea and can use the different pictures that children create to provoke a discussion about mathematical ideas. Constructing their own pictures can be a powerful learning experience for children because they must consider several aspects of mathematical ideas that are often assumed when pictures are pre-drawn for students.

Physical: The manipulatives representation refers to the unifix cubes, base-ten blocks, fraction circles, and the like, that a child might use to solve a problem. Because children can physically manipulate these objects, when used appropriately, they provide opportunities to compare relative sizes of objects, to identify patterns, as well as to put together representations of numbers in multiple ways.

Verbal: Traditionally, teachers often used the spoken language of mathematics but rarely gave students opportunities to grapple with it. Yet, when students do have opportunities to express their mathematical reasoning aloud, they may be able to make explicit some knowledge that was previously implicit for them.

Symbolic: Written symbols refer to both the mathematical symbols and the written words that are associated with them. For students, written symbols tend to be more abstract than the other representations. I tend to introduce symbols after students have had opportunities to make connections among the other representations, so that the students have multiple ways to connect the symbols to mathematical ideas, thus increasing the likelihood that the symbols will be comprehensible to students.

Contextual: A relevant situation can be any context that involves appropriate mathematical ideas and holds interest for children; it is often, but not necessarily, connected to a real-life situation.

The Lesh Translation Model: Importance of Connections

As important as the ovals are in this model, another feature of the model is even more important than the representations themselves: The arrows! The arrows are important because they represent the connections students make between the representations. When students make these connections, they may be better able to access information about a mathematical idea, because they have multiple ways to represent it and, thus, many points of access.

Individuals enhance or modify their knowledge by building on what they already know, so the greater the number of representations with which students have opportunities to engage, the more likely the teacher is to tap into a student's prior knowledge. This "tapping in" can then be used to connect students' experiences to those representations that are more abstract in nature (such as written symbols). Not all students have the same set of prior experiences and knowledge. Teachers can introduce multiple representations in a meaningful way so that students' opportunities to grapple with mathematical ideas are greater than if their teachers used only one or two representations.

Concrete Pictorial Abstract (CPA) Instructional Approach

The CPA approach suggests that there are three steps necessary for pupils to develop understanding of a mathematical concept.

Concrete: "Doing Stage": Physical manipulation of objects to solve math problems.

Pictorial: "Seeing Stage": Use of imaged to represent objects when solving math problems.

Abstract: "Symbolic Stage": Use of only numbers and symbols to solve math problems.

CPA is a gradual systematic approach. Each stage builds on to the previous stage. Reinforcement of concepts are achieved by going back and forth between these representations and making connections between stages. Students will benefit from seeing parallel samples of each stage and how they transition from one to another.

Read, Draw, Write Process

READ the problem. Read it over and over.... And then read it again.

DRAW a picture that represents the information given. During this step students ask themselves: Can I draw something from this information? What can I draw? What is the best model to show the information? What conclusions can I make from the drawing? **WRITE** your conclusions based on the drawings. This can be in the form of a number sentence, an equation, or a statement.

Students are able to draw a model of what they are reading to help them understand the problem. Drawing a model helps students see which operation or operations are needed, what patterns might arise, and which models work and do not work. Students must dive deeper into the problem by drawing models and determining which models are appropriate for the situation.

While students are employing the RDW process they are using several Standards for Mathematical Practice and in some cases, all of them.

Mathematical Discourse and Strategic Questioning

Discourse involves asking strategic questions that elicit from students their understanding of the context and actions taking place in a problem, how a problem is solved and why a particular method was chosen. Students learn to critique their own and others' ideas and seek out efficient mathematical solutions.

While classroom discussions are nothing new, the theory behind classroom discourse stems from constructivist views of learning where knowledge is created internally through interaction with the environment. It also fits in with socio-cultural views on learning where students working together are able to reach new understandings that could not be achieved if they were working alone.

Underlying the use of discourse in the mathematics classroom is the idea that mathematics is primarily about reasoning not memorization. Mathematics is not about remembering and applying a set of procedures but about developing understanding and explaining the processes used to arrive at solutions.

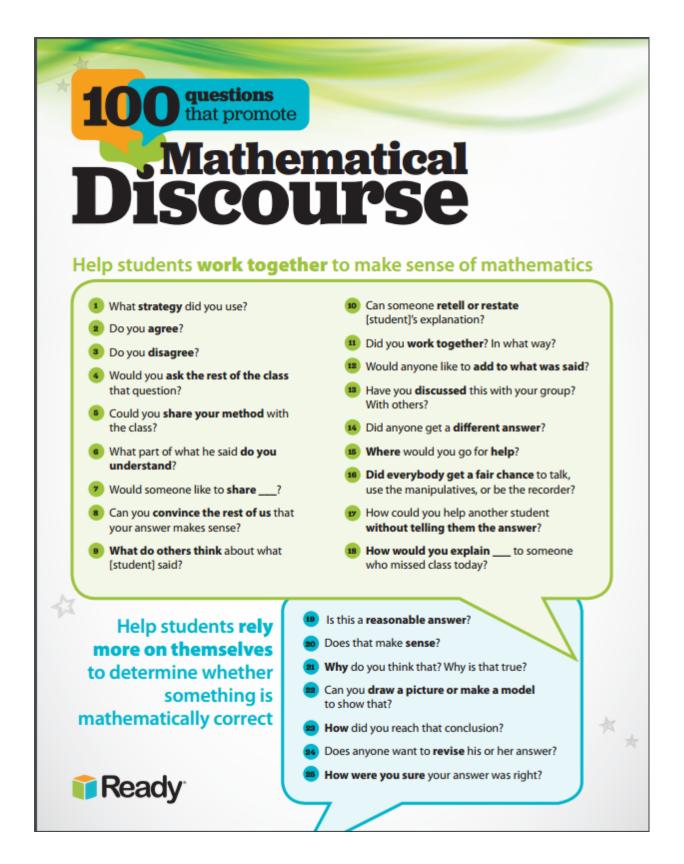
Teacher Questioning:

Asking better questions can open new doors for students, promoting mathematical thinking and classroom discourse. Can the questions you're asking in the mathematics classroom be answered with a simple "yes" or "no," or do they invite students to deepen their understanding?



Albert Einstein

To help you encourage deeper discussions, here are 100 questions to incorporate into your instruction by Dr. Gladis Kersaint, mathematics expert and advisor for Ready Mathematics.



Help students learn to reason mathematically

- How did you begin to think about this problem?
- What is another way you could solve this problem?
- How could you prove ____
- Can you explain how your answer is different from or the same as [student]'s answer?
- Let's break the problem into parts. What would the parts be?
- Can you explain this part more specifically?
- Does that always work?
- Can you think of a case where that wouldn't work?
- 34 How did you organize your information? Your thinking?

Help students with problem comprehension

Help students evaluate their own processes and engage in productive peer interaction

- What do you need to do next?
- 36 What have you accomplished?
- What are your strengths and weaknesses?
- Was your group participation appropriate and helpful?
 - What is this problem about? What can you tell me about it?
 - O Do you need to define or set limits for the problem?
 - How would you interpret that?
 - Could you reword that in simpler terms?
 - 43 Is there something that can be eliminated or that is missing?
 - Could you explain what the problem is asking?
 - What assumptions do you have to make?
 - What do you know about this part?
 - Which words were most important? Why?



100 Questions That Promote Mathematical Discourse 2



Help students learn to conjecture, invent, and solve problems

- What would happen if ___?
- Do you see a pattern?
- What are some possibilities here?
- Where could you find the information you need?
- How would you check your steps or your answer?
- What did not work?
- How is your solution method the same as or different from [student]'s method?
- Other than retracing your steps, how can you determine if your answers are appropriate?
- 66 How did you organize the information? Do you have a record?
- How could you solve this using tables, lists, pictures, diagrams, etc.?
- What have you tried? What steps did you take?
- 69 How would it look if you used this model or these materials?

- How would you draw a diagram or make a sketch to solve the problem?
- 61 Is there another possible answer? If so, explain.
- Is there another way to solve the problem?
- Is there another model you could use to solve the problem?
- Is there anything you've overlooked?
- How did you think about the problem?
- 66 What was your estimate or prediction?
- How confident are you in your answer?
- What else would you like to know?
- What do you think comes next?
- Is the solution reasonable, considering the context?
- Did you have a system? Explain it.
- Did you have a strategy? Explain it.
- Did you have a design? Explain it.





100 Questions That Promote Mathematical Discourse 3

Help students learn to connect mathematics, its ideas, and its application

- What is the relationship between ____
- Have we ever solved a problem like this before?
- What uses of mathematics did you find in the newspaper last night?
- What is the same?
- What is different?
- Did you use skills or build on concepts that were not necessarily mathematical?
- Which skills or concepts did you use?
- What ideas have we explored before that were useful in solving this problem?

- Is there a pattern?
- Where else would this strategy be useful?
- How does this relate to ?
- Is there a general rule?
- Is there a real-life situation where this could be used?
- How would your method work with other problems?
- What other problem does this seem to lead to?
 - Have you tried making a guess?
 - What else have you tried?
 - Would another method work as well or better?
 - 92 Is there another way to draw, explain, or say that?
 - Give me another related problem. Is there an easier problem?
 - How would you explain what you know right now?

Help students persevere

- What was one thing you learned (or two, or more)?
- Did you notice any patterns? If so, describe them.
- What mathematics topics were used in this investigation?
- What were the mathematical ideas in this problem?
- What is mathematically different about these two situations?
- What are the variables in this problem? What stays constant?

Help students focus on the mathematics from activities

Ready

100 Questions That Promote Mathematical Discourse 4

Conceptual Understanding

Students demonstrate conceptual understanding in mathematics when they provide evidence that they can:

- recognize, label, and generate examples of concepts;
- use and interrelate models, diagrams, manipulatives, and varied representations of concepts;
- identify and apply principles; know and apply facts and definitions;
- compare, contrast, and integrate related concepts and principles; and
- recognize, interpret, and apply the signs, symbols, and terms used to represent concepts.

Conceptual understanding reflects a student's ability to reason in settings involving the careful application of concept definitions, relations, or representations of either.

Procedural Fluency

Procedural fluency is the ability to:

- apply procedures accurately, efficiently, and flexibly;
- to transfer procedures to different problems and contexts;
- to build or modify procedures from other procedures; and
- to recognize when one strategy or procedure is more appropriate to apply than another.

Procedural fluency is more than memorizing facts or procedures, and it is more than understanding and being able to use one procedure for a given situation. Procedural fluency builds on a foundation of conceptual understanding, strategic reasoning, and problem solving (NGA Center & CCSSO, 2010; NCTM, 2000, 2014). Research suggests that once students have memorized and practiced procedures that they do not understand, they have less motivation to understand their meaning or the reasoning behind them (Hiebert, 1999). Therefore, the development of students' conceptual understanding of procedures should precede and coincide with instruction on procedures.

Math Fact Fluency: Automaticity

Students who possess math fact fluency can recall math facts with automaticity. Automaticity is the ability to do things without occupying the <u>mind</u> with the low-level details required, allowing it to become an automatic response pattern or <u>habit</u>. It is usually the result of <u>learning</u>, <u>repetition</u>, and practice.

K-2 Math Fact Fluency Expectation

K.OA.5 Add and Subtract within 5.

1.0A.6 Add and Subtract within 10.

2.0A.2 Add and Subtract within 20.

Math Fact Fluency: Fluent Use of Mathematical Strategies

First and second grade students are expected to solve addition and subtraction facts using a variety of strategies fluently.

1.0A.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10.

Use strategies such as:

- counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14);
- decomposing a number leading to a ten (e.g., 13 4 = 13 3 1 = 10 1 = 9);
- using the relationship between addition and subtraction; and
- creating equivalent but easier or known sums.

2.NBT.7 Add and subtract within 1000, using concrete models or drawings and strategies based on:

- o place value,
- o properties of operations, and/or
- o the relationship between addition and subtraction;

Evidence of Student Thinking

Effective classroom instruction and more importantly, improving student performance, can be accomplished when educators know how to elicit evidence of students' understanding on a daily basis. Informal and formal methods of collecting evidence of student understanding enable educators to make positive instructional changes. An educators' ability to understand the processes that students use helps them to adapt instruction allowing for student exposure to a multitude of instructional approaches, resulting in higher achievement. By highlighting student thinking and misconceptions, and eliciting information from more students, all teachers can collect more representative evidence and can therefore better plan instruction based on the current understanding of the entire class.

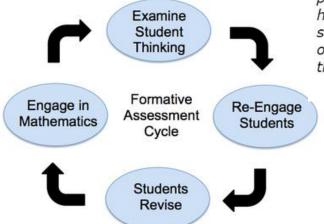
Mathematical Proficiency

To be mathematically proficient, a student must have:

- <u>Conceptual understanding</u>: comprehension of mathematical concepts, operations, and relations;
- <u>Procedural fluency</u>: skill in carrying out procedures flexibly, accurately, efficiently, and appropriately;
- <u>Strategic competence</u>: ability to formulate, represent, and solve mathematical problems;
- <u>Adaptive reasoning</u>: capacity for logical thought, reflection, explanation, and justification;
- <u>Productive disposition</u>: habitual inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one's own efficacy.

Evidence should:

- Provide a window in student thinking;
- Help teachers to determine the extent to which students are reaching the math learning goals; and
- Be used to make instructional decisions during the lesson and to prepare for subsequent lessons.



Formative assessment is an essentially interactive process, in which the teacher can find out whether what has been taught has been learned, and if not, to do something about it. Day-to-day formative assessment is one of the most powerful ways of improving learning in the mathematics classroom.

(Wiliam 2007, pp. 1054; 1091)

Connections to the Mathematical Practices

Student Friendly Connections to the Mathematical Practices

- 1. I can solve problems without giving up.
- 2. I can think about numbers in many ways.
- 3. I can explain my thinking and try to understand others.
- 4. I can show my work in many ways.
- 5. I can use math tools and tell why I choose them.
- 6. I can work carefully and check my work.
- 7. I can use what I know to solve new problems.
- 8. I can discover and use short cuts.

ards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their
hey solved them. Students will begin to explain the meaning of a problem, and look for ways to solve it. Kindergarteners will learn learn. When working in small groups or with a partner they will listen to the strategies of the group and will try different approach
ps while solving tasks. This involves two processes- decontextualizing and contextualizing.
abols. For example, in the task, "There are 7 children on the playground and some children go line up. If there are 4 children still pla
olving the task above, students refer to the context of the task to determine that they need to subtract 4 since the number of childre
ruct arguments and engage in discussions about problem solving strategies. For example, while solving the task, "There are 8 books ent about why they subtracted 3 form 8 rather than adding 8 and 3. Further, Kindergarten students are expected to examine a varie

a number sentence or an equation, and check to make sure that their equation accurately matches the problem context. g tasks, but the expectation is that they will also write an equation to model problem situations.
w many are left?" Kindergarten students are expected to write the equation $7-3=4$.
n equation.
hese tools may include counters, place value (base ten) blocks, hundreds number boards, number lines, and concrete geometric sl al understanding.
as paper, and determine which tools are the most appropriate to use. For example, while solving the task "There are 4 dogs in the
ons, and measurements. In all mathematical tasks, students in Kindergarten describe their actions and strategies clearly, using gra
there are no gaps or overlaps. During tasks involving number sense, students check their work to ensure the accuracy and reason

the number system and other areas of mathematics. While solving addition problems, students begin to recognize the commutativ
e decomposed into 10 and some leftovers, such as $12 = 10+2$, $13 = 10+3$, etc.
work with subtraction as missing addend problems, such as $5-1 = $ can be written as $1+$ $= 5$ and can be thought of as how much
cures when solving mathematical tasks.
ui es when solving mathematical tasks.
nany of each could there be?"
+4=8), 5 of one color and 3 of another $(5+3=8)$, etc.
ined to equal 8.

Effective Mathematics Teaching Practices

Establish mathematics goals to focus learning. Effective teaching of mathematics establishes clear goals for the mathematics that students are learning, situates goals within learning progressions, and uses the goals to guide instructional decisions.

Implement tasks that promote reasoning and problem solving. Effective teaching of mathematics engages students in solving and discussing tasks that promote mathematical reasoning and problem solving and allow multiple entry points and varied solution strategies.

Use and connect mathematical representations. Effective teaching of mathematics engages students in making connections among mathematical representations to deepen understanding of mathematics concepts and procedures and as tools for problem solving.

Facilitate meaningful mathematical discourse. Effective teaching of mathematics facilitates discourse among students to build shared understanding of mathematical ideas by analyzing and comparing student approaches and arguments.

Pose purposeful questions. Effective teaching of mathematics uses purposeful questions to assess and advance students' reasoning and sense making about important mathematical ideas and relationships.

Build procedural fluency from conceptual understanding. Effective teaching of mathematics builds fluency with procedures on a foundation of conceptual understanding so that students, over time, become skillful in using procedures flexibly as they solve contextual and mathematical problems.

Support productive struggle in learning mathematics. Effective teaching of mathematics consistently provides students, individually and collectively, with opportunities and supports to engage in productive struggle as they grapple with mathematical ideas and relationships.

Elicit and use evidence of student thinking. Effective teaching of mathematics uses evidence of student thinking to assess progress toward mathematical understanding and to adjust instruction continually in ways that support and extend learning.

5 Pract	ices for Orchestrating Productive Mathematics Discussions
Practice	Description/ Questions
1. Anticipating	What strategies are students likely to use to approach or solve a challenging high-level mathematical task?
	How do you respond to the work that students are likely to produce?
	Which strategies from student work will be most useful in addressing the mathematical goals?
2. Monitoring	Paying attention to what and how students are thinking during the lesson.
	Students working in pairs or groups
	Listening to and making note of what students are discussing and the strategies they are using
	Asking students questions that will help them stay on track or help them think more deeply about the task. (Promote productive struggle)
3. Selecting	This is the process of deciding the <i>what</i> and the <i>who</i> to focus on during the discussion.
	Selection of children is guided by the mathematical goal for the lesson
4. Sequencing	What order will the solutions be shared with the class?
	Sequence depends largely on the teacher's goals for a lesson
	Maximizing the chances that math goals will be achieved
5. Connecting	Asking the questions that will make the mathematics explicit and understandable.
	Focus must be on mathematical meaning and relationships; making links between mathematical ideas and representations.

MATH CENTERS/ WORKSTATIONS

Math workstations allow students to engage in authentic and meaningful hands-on learning. They often last for several weeks, giving students time to reinforce or extend their prior instruction. Before students have an opportunity to use the materials in a station, introduce them to the whole class, several times. Once they have an understanding of the concept, the materials are then added to the work stations.

Station Organization and Management Sample

Teacher A has 12 containers labeled 1 to 12. The numbers correspond to the numbers on the rotation chart. She pairs students who can work well together, who have similar skills, and who need more practice on the same concepts or skills. Each day during math work stations, students use the center chart to see which box they will be using and who their partner will be. Everything they need for their station will be in their box. **Each station is differentiated**. If students need more practice and experience working on numbers 0 to 10, those will be the only numbers in their box. If they are ready to move on into the teens, then she will place higher number activities into the box for them to work with.



In the beginning there is a lot of prepping involved in gathering, creating, and organizing the work stations. However, once all of the initial work is complete, the stations are easy to manage. Many of her stations stay in rotation for three or four weeks to give students ample opportunity to master the skills and concepts.

Read *Math Work Stations* by Debbie Diller.

In her book, she leads you step-by-step through the process of implementing work stations.

MATH WORKSTATION INFORMATION CARD

ath Workstation:		 Time:
JSLS.:		
	this task, I will be able to:	
•		
sk(s): •		
•		
•		
•		
•it Ticket:		

MATH WORKSTATION SCHEDULE

Week	of:
110012	$\mathbf{O}_{\mathbf{I}}$

DAY	Technology	Problem Solving Lab	Fluency	Math	Small Group Instruc-
	Lab		Lab	Journal	tion
Mon.					
	Group	Group	Group	Group	BASED
Tues.					ON CURRENT
	Group	Group	Group	Group	OBSERVATIONAL
Wed.					DATA
	Group	Group	Group	Group	
Thurs.					
	Group	Group	Group	Group	
Fri.					
	Group	Group	Group	Group	

INSTRUCTIONAL GROUPING

INSTRUCTIONAL GROUPING					
	GROUP A		GROUP B		
1		1			
2		2			
3		3			
4		4			
5		5			
6		6			
	GROUP C		GROUP D		
1		1			
2		2			
3		3			
4		4			
5		5			
6		6			

Kindergarten PLD Rubric

Co	+ I+	Not There Yet			
Got It Evidence shows that the student essentially has the target con-		Student shows evidence of a mai		oncents or procedure or a fail-	
cept or big math idea.		Student shows evidence of a major misunderstanding, incorrect concepts or procedure, or a failure to engage in the task.			
PLD Level 5: 100% PLD Level 4: 89%		PLD Level 3: 79%	PLD Level 2: 69%	PLD Level 1: 59%	
Distinguished command	Strong Command	Moderate Command	Partial Command	Little Command	
Student work shows distin -	Student work shows strong	Student work shows moderate	Student work shows partial	Student work shows little un-	
guished levels of understand-	levels of understanding of the	levels of understanding of the	understanding of the mathe-	derstanding of the mathemat-	
ing of the mathematics.	mathematics.	mathematics.	matics.	ics.	
Student constructs and com-	Student constructs and com-	Student constructs and com-	Student constructs and com-	Student attempts to constructs	
municates a complete re-	municates a complete re-	municates a complete response	municates an incomplete re-	and communicates a response	
sponse based on explana-	sponse based on explana-	based on explana-	sponse based on student's at-	using the:	
tions/reasoning using the:	tions/reasoning using the:	tions/reasoning using the:	tempts of explanations/ rea-	Tools:	
• Tools:	• Tools:	Tools:	soning using the:	 Manipulatives 	
 Manipulatives 	 Manipulatives 	 Manipulatives 	Tools:	o Five Frame	
o Five Frame	o Five Frame	o Five Frame	 Manipulatives 	o Ten Frame	
o Ten Frame	o Ten Frame	o Ten Frame	o Five Frame	 Number Line 	
 Number Line 	 Number Line 	 Number Line 	o Ten Frame	o Part-Part-Whole	
o Part-Part-Whole	o Part-Part-Whole	o Part-Part-Whole	o Number Line	Model	
Model	Model	Model	o Part-Part-Whole	Strategies:	
Strategies:	Strategies:	Strategies:	Model	 Drawings 	
o Drawings	o Drawings	o Drawings	• Strategies:	o Counting All	
o Counting All	o Counting All	o Counting All	o Drawings	o Count On/Back	
o Count On/Back	o Count On/Back	o Count On/Back	o Counting All	 Skip Counting 	
o Skip Counting	o Skip Counting	o Skip Counting	o Count On/Back	o Making Ten	
o Making Ten	o Making Ten	o Making Ten	Skip Counting Making Trans	o Decomposing	
DecomposingNumber	DecomposingNumber	DecomposingNumber	o Making Ten	Number	
		Number Precise use of math vo-	DecomposingNumber	Precise use of math vo- cabulary	
Precise use of math vo- cabulary	Precise use of math vo- cabulary	cabulary	Precise use of math vo-	Cabulary	
Response includes an efficient	Cabulal y	Cabulary	cabulary	Response includes limited evi-	
and logical progression of	Response includes a logical	Response includes a logical but	Cabulat y	dence of the progression of	
mathematical reasoning and	progression of mathematical	incomplete progression of	Response includes an incom-	mathematical reasoning and	
understanding.	reasoning and understanding.	mathematical reasoning and	plete or illogical progression of	understanding.	
	a same and a same and a same and a same a sa	understanding.	mathematical reasoning and		
		Contains minor errors .	understanding.		
5 points	4 points	3 points	2 points	1 point	

DATA DRIVEN INSTRUCTION

Formative assessments inform instructional decisions. Taking inventories and assessments, observing reading and writing behaviors, studying work samples and listening to student talk are essential components of gathering data. When we take notes, ask questions in a student conference, lean in while a student is working or utilize a more formal assessment we are gathering data. Learning how to take the data and record it in a meaningful way is the beginning of the cycle.

Analysis of the data is an important step in the process. What is this data telling us? We must look for patterns, as well as compare the notes we have taken with work samples and other assessments. We need to decide what are the strengths and needs of individuals, small groups of students and the entire class. Sometimes it helps to work with others at your grade level to analyze the data.

Once we have analyzed our data and created our findings, it is time to make informed instructional decisions. These decisions are guided by the following questions:

- What mathematical practice(s) and strategies will I utilize to teach to these needs?
- What sort of grouping will allow for the best opportunity for the students to learn what it is I see as a need?
- Will I teach these strategies to the whole class, in a small guided group or in an individual conference?
- Which method and grouping will be the most effective and efficient? What specific objective(s) will I be teaching?

Answering these questions will help inform instructional decisions and will influence lesson planning.

Then we create our instructional plan for the unit/month/week/day and specific lessons.

It's important now to reflect on what you have taught.

Did you observe evidence of student learning through your checks for understanding, and through direct application in student work?

What did you hear and see students doing in their reading and writing?

Now it is time to begin the analysis again.



Data Analysis Form S	chool:		Date:	
Assessment:		NJSLS:		
		·		
GROUPS (STUDENT INITIALS)	SUPPORT PLAN		PROGRESS	
MASTERED (86% - 100%) (PLD 4/5):				
DEVELOPING (67% - 85%) (PLD 3):				
INSECURE (51%-65%) (PLD 2):				
BEGINNING (0%-50%) (PLD 1):				

MATH PORTFOLIO EXPECTATIONS

The Student Assessment Portfolios for Mathematics are used as a means of documenting and evaluating students' academic growth and development over time and in relation to the CCSS-M. The September task entry(-ies) should reflect the prior year content and *can serve* as an additional baseline measure.

All tasks contained within the **Student Assessment Portfolios** should be aligned to NJSLS and be "practice forward" (closely aligned to the Standards for Mathematical Practice).

Four (4) or more additional tasks will be included in the **Student Assessment Portfolios** for Student Reflection and will be labeled as such.

K-2 GENERAL PORTFOLIO EXPECTATIONS:

- Tasks contained within the Student Assessment Portfolios are "practice forward" and denoted as "Individual", "Partner/Group", and "Individual w/Opportunity for Student Interviews¹.
- Each Student Assessment Portfolio should contain a "Task Log" that documents all tasks, standards, and rubric scores aligned to the performance level descriptors (PLDs).
- Student work should be attached to a completed rubric; with appropriate teacher feedback on student work.
- Students will have multiple opportunities to revisit certain standards. Teachers will capture each additional opportunity "as a new and separate score" in the task log.
- A 2-pocket folder for each Student Assessment Portfolio is *recommended*.
- All Student Assessment Portfolio entries should be scored and recorded as an Authentic Assessment grade (25%)².
- All Student Assessment Portfolios must be clearly labeled, maintained for all students, inclusive of constructive teacher and student feedback and accessible for review.

GRADES K-2

Student Portfolio Review

Provide students the opportunity to review and evaluate their portfolio at various points throughout the year; celebrating their progress and possibly setting goals for future growth. During this process, students should retain ALL of their current artifacts in their Mathematics Portfolio.

Resources

Number Book Assessment Link: http://investigations.terc.edu/

Model Curriculum- http://www.nj.gov/education/modelcurriculum/

Georgia Department of Education: Games to be played at centers with a partner or small group. http://ccgpsmathematicsk-5.wikispaces.com/Kindergarten

Engage NY: *For additional resources to be used during centers or homework.

https://www.engageny.org/sites/default/files/resource/attachments/math-gk-m1-full-module.pdf

Add/ Subtract Situation Types: Darker Shading indicates Kindergarten expectations https://achievethecore.org/content/upload/Add%20Subtract%20Situation%20Types.pdf

Math in Focus PD Videos: https://www-

 $\underline{k6.thinkcentral.com/content/hsp/math/hspmath/common/mif_pd_vid/9780547760346_te/index.}$ \underline{html}

Number Talks activities: psassets.weebly.com/uploads/9/9/3/2/.../number_talks_kindergarten_resource.pdf

Suggested Literature

Fish Eyes by, Lois Ehlert

Ten Little Puppies by, Elena Vazquez

Zin! Zin! Zin! A Violin! by, Lloyd Moss

My Granny Went to the Market by, Stella Blackstone and Christopher Corr

Anno's Couting Book by, Mitsumasa Anno

Chicka, Chicka, 1,2,3 by, Bill Martin Jr.; Michael Sampson; Lois Ehlert

How Dinosaurs Count to 10 by Jane Yolen and Mark Teague

10 Little Rubber Ducks by Eric Carle

Ten Black Dots by Donald Crews

Mouse Count by Ellen Stoll Walsh

Count! by Denise Fleming

21st Century Career Ready Practices

- CRP1. Act as a responsible and contributing citizen and employee.
- CRP2. Apply appropriate academic and technical skills.
- CRP3. Attend to personal health and financial well-being.
- CRP4. Communicate clearly and effectively and with reason.
- CRP5. Consider the environmental, social and economic impacts of decisions.
- CRP6. Demonstrate creativity and innovation.
- CRP7. Employ valid and reliable research strategies.
- CRP8. Utilize critical thinking to make sense of problems and persevere in solving them.
- CRP9. Model integrity, ethical leadership and effective management.
- CRP10. Plan education and career paths aligned to personal goals.
- CRP11. Use technology to enhance productivity.
- CRP12. Work productively in teams while using cultural global competence.

For additional details see 21st Century Career Ready Practices .

References

"Eureka Math" Great Minds. 2018 < https://greatminds.org/account/products>